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Representation of results of particle size analysis —

Part 3: Adjustment of an experimental curve to a reference model

Représentation de données obtenues par analyse granulométrique — Partie 3: Ajustement d'une courbe expérimentale à un modèle de référence



Reference number ISO 9276-3:2008(E)

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Foreword

ISO (the International Organization for Standardization) is a worldwide federation of national standards bodies (ISO member bodies). The work of preparing International Standards is normally carried out through ISO technical committees. Each member body interested in a subject for which a technical committee has been established has the right to be represented on that committee. International organizations, governmental and non-governmental, in Maison with ISO, also take part in the work. ISO collaborates closely with the International Electrotechnical Commission (IEC) on all matters of electrotechnical standardization.

International Standards are drafted in accordance with the rules given in the ISO/IEC Directives, Part 2.

The main task of technical committees is to prepare International Standards. Draft International Standards adopted by the technical committees are circulated to the member bodies for voting. Publication as an International Standard requires approval by at least 75 % of the member bodies casting a vote.

Attention is drawn to the possibility that some of the elements of this document may be the subject of patent rights. ISO shall not be held responsible for identifying any or all such patent rights.

ISO 9276-3 was prepared by Technical Committee ISO/TC 24, *Sieves, sieving and other sizing methods*, Subcommittee SC 4, *Sizing by methods other than sieving*.

ISO 9276 consists of the following parts, under the general title Representation of results of particle size analysis:

- Part 1: Graphical representation
- Part 2: Calculation of average particle sizes/diameters and moments from particle size distributions
- Part 3: Adjustment of an experimental curve to a reference mod
- Part 4: Characterization of a classification process
- Part 5: Methods of calculation relating to particle size analyses using logarithmic normal probability distribution

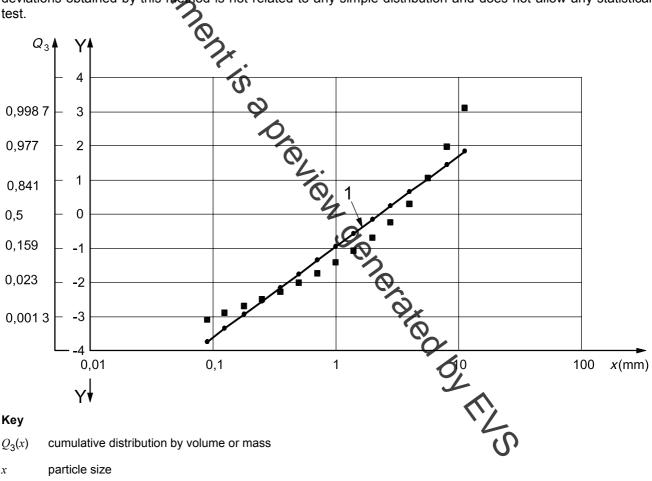
The following part is under preparation:

— Part 6: Descriptive and quantitative representation of particle shape and morphology

Introduction

Cumulative curves of particle size distributions are sigmoids, therefore fitting to a model distribution function or rendering statistical intercomparison is difficult. These disadvantages can, however, be remedied by transforming these sigmoids into straight lines by means of appropriate coordinate systems, e.g. log-normal, Rosin-Rammler or Gates-Gaudin-Schuhmann (log-log). Target size distributions in particle technology industries can also be described in terms of distribution models.

In such systems, conclassic linear regression assumes that the squares of the deviations between the experimental points and the theoretical straight line are, on average, equal. This is only valid in the transformed cumulative distribution value system, but not in their linear representation, and therefore named a quasilinear regression. In particular, the scale extension makes the values of the squares of the deviations at the extremities of the graph yary by several orders of magnitude. In addition, the sum of the squares of the deviations obtained by this method is not related to any simple distribution and does not allow any statistical test.



- $Q_3(x)$
- particle size x
- Y quantiles of the standard normal distribution
- 1 quasilinear regression full line
- quasilinear fit point
- $Q_3(x)$ data point

Figure 1 — Example of a functional paper with log-normal plot (cumulative distribution values plotted on a normal ordinate against particle size on a logarithmic abscissa with inverse standard normal distribution transformed) and guasilinear regression full line

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Representation of results of particle size analysis -

Part 3:

Adjustment of an experimental curve to a reference model

1 Scope

This part of ISO 9276 specifies methods for the adjustment of an experimental curve to a reference model with respect to a statistical background. Furthermore, the evaluation of the residual deviations, after the adjustment, is also specified. The reference model can also serve as a target size distribution for maintaining product quality.

This part of ISO 9276 specifies procedures that are applicable to the following reference models:

- a) normal distribution (Laplace-Gauss) powders obtained by precipitation, condensation or natural products (pollens);
- b) log-normal distribution (Galton MacAlister powders obtained by grinding or crushing;
- c) Gates-Gaudin-Schuhmann distribution (bilogarithmic): analysis of the extreme values of the fine particle distributions;
- d) Rosin-Rammler distribution: analysis of the extremevalues of the coarse particle distributions;
- e) any other model or combination of models, if a non-linear fit method is used (see bimodal example in Annex C).

This part of ISO 9276 can substantially support product quality assurance or process optimization related to particle size distribution analysis.

2 Normative references

The following referenced documents are indispensable for the application of this document. For dated references, only the edition cited applies. For undated references, the latest edition of the referenced document (including any amendments) applies.

ISO 9276-2, Representation of results of particle size analysis — Part 2: Calculation of average particle sizes/diameters and of moments from particle size distributions

ISO 9276-5, Representation of results of particle size analysis — Part 5: Methods of calculation relating to particle size analyses using logarithmic normal probability distribution